

Errata for Stakgold Boundary Value Problems of Mathematical Physics

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These errata are for the following two books, both blue-covered hardbacks in the Macmillan Series in Advanced Mathematics and Theoretical Physics,

I. Stakgold, *Boundary Value Problems of Mathematical Physics*

Volume I, 1967, sixth printing 1972 (Macmillan, London) (Chapters 1 through 4)

Volume II, 1968, second printing 1971 (Macmillan, London) (Chapters 5 through 8)

The books were reprinted in 2000 in a SIAM edition with corrections, but some errata managed to escape detection as noted below.

These "errata" are just items I happened to notice while working my way through the first 7 chapters of this two volume set (Chapter 8 will have to wait). I bought these books in 1972 while taking Math 224 at UC Berkeley, but only recently was I able to find time to read them!

My reasons for creating this errata list are as follows:

- (1) these wonderful books should be preserved indefinitely in the best possible working condition.
- (2) The books are excellent but are also somewhat difficult in places, requiring the reader to do many calculational steps between "waypoints" given by the author. When there are errors in those waypoints, the student having a finite amount of time may give up or at least be quite discouraged.
- (3) Someone who borrows these volumes from a library is likely to get the original editions, not the new editions which have most items corrected.
- (4) Even the new 2000 editions continue to have some errata.
- (5) I could find no existing errata on line.

I understand probably better than most why the author decided to put out a more condensed version of the book (called *Green's Functions and Boundary Value Problems* now in a 3rd edition Wiley 2011) which "could be covered in a one-year course" as he says in his Preface. Ah, but if you really want to know the nuts and bolts inside the machine, I would recommend the long version.

Any of my errata of course could be erroneous, for which I apologize ahead of time. Some errata are trivial typos hardly worth mentioning, but since I marked them in my book, they might as well get recorded here.

An asterisk * after the page number indicates an erratum not fixed in the 2000 SIAM edition.

Volume I.

Chapter 1

none

Chapter 2

p 136* 9th line down should say We are to show $T[x_n] \rightarrow T[x]$ // not $\rightarrow [Tx]$

p 146 4th line from the bottom should say in (2.34) below // not (2.33)

p 163 5th line from bottom should say $I_4[\phi_1] = |\mu_1|$ // not $= |\lambda_1|$

p 176 first line should say $\int_0^t du [y(u) \dots$ // not $\int_0^t dt [y(u) \dots$

p 176* equ (IV) at bottom should say $y(1) = 0$ // not $x(1) = 0$

p 184 mid page should say The second boundary....if $0 = \int_0^1 e^{-\lambda \xi} f(\xi) d\xi$. // not $\int_0^t$

Chapter 3

p 204 2nd last line should say ..for the solution of the inhomogeneous ... // not homogeneous

Chapter 4

p 299* equ (4.83a) β_0 in last term should be b_0 to match b_0 in (4.82a) and earlier discussion.
This was changed in 2000 so that all terms show β_0 , but all should show b_0 .

p 303* last equ should have $\hat{g} = -(\alpha_1^2 + \alpha_2^2)^{-1} [\psi \dots$ // not $(\alpha_1^2 + \alpha_2^2) [\psi$

p 314* 2nd para should begin Each possible... of A in (4.125a) yields // not of A is (4.125a)

p 315 1st equ bracket factor should be $[\gamma + \log(\sqrt{\lambda}/2)]$ // not $[(\gamma + \log(\sqrt{\lambda}))/2]$

p 315* 1st equ in Ex 4.26 should have ρ replaced by x in two places so then has $x_<$ and $x_>$.

Volume II

Chapter 5

p 38* 2nd equ in Ex 5.18 should have factor $(-iu)^P$ // not $(-iu)^n$

p 56 last equ on page, integration variable should be $d\alpha_n$ // not $d\alpha$

Chapter 6

p 94 below equation number (6.10) should read expression // not expression

p 131 equ (6.75) should begin with $g(x|\xi) =$ // not $g(x)|\xi) =$

p 132 Theorem 4 in bold type should read Theorem 3 (Theorem 4 is on page 133).

p 144 Ex 6.30, 6th line up from bottom should say $Z = \sqrt{z} R$ // not $Z = zR$

p 145* 2nd equation should say $u_{m,n,k} = (1/\sqrt{r}) J_{n+(1/2)}$ // not $(1/r) J_{n+(1/2)}$

p 147 1st equ after EXAMPLE should end with $= -(1/4\pi) \log(1+r^2-2r\cos\theta)$ // log is missing

p 158 2nd equ on page (one after Thus) is missing a factor $\sin(m\pi x/a)$, but OK in (6.117).

p 161* Eq (6.122) integration variable should be $d\alpha$ and not dx .

p 165* 2nd last equ begins $w\bar{w} = E\bar{E}$ (num/denom) : last signs in both num and denom should be + instead of -.

p 166* Ex 6.36 should say By the calculus of residues // not calculus residues

p 166 last equ should have integration variable $d\alpha$ // not $d\xi$

p 168* equ (6.132) left side should read $g(r,\phi | r_0,0) =$ // not $g(r,\theta | r_0,0) =$

p 171 equ (6.137) left side should read $h(r,\phi | r_0, 0) = A + \dots$ // not $h(r,\phi | r_0, \phi_0)$

p 179* 3rd line of text should say According to (6.195) in Exercise 6.47
and not According to (6.192) in Exercise 6.48 two typos here
the second typo is fixed in the 2000 SIAM edition

p 179* 5th equ, last bracket should be $[c_0 - (1/2\pi) \log a]$ // not $[c_0 (1/2\pi) \log a]$

p 183* 4th equ bracket should be $[\frac{R^2-r_0^2}{2a} + \frac{a}{2}]$ // not $[\frac{R^2-r_0^2}{2} + \frac{a}{2}]$

p 183* 5th equ should say $I(s) = -\frac{1}{4\pi a R^3} [..]$ // not $I(s) = -\frac{1}{4\pi R^3} [..]$

p 187* last equ on page should read $u(s-) - u_i(s-) =$ // not $u(s-) - u_i s-) =$

Chapter 7

- p 213 1st sentence after heading should say for the heat equation // not equaton
- p 218 6th line of text should say Alternatively, we use (7.57) // not (7.47)
- p 218 2nd last equ should have $\tilde{q}(x,s) + f(x)$ // not $\tilde{g}(x,s)$
- p 230 1st equ should have factor $(2/\ell)$ before the Σ // as in equ (7.50)
- p 237* 4th line of text should say of strength $4\pi/3$ // not strength 4π
- p 240 Ex 7.10 equ should have factor $\frac{4\pi n}{\ell^2}$ // not $\frac{4\pi n}{\ell}$
- p 242* 3rd line of text above Ex 7.17 should say Fourier sine transform // not cosine transform
- p 242* last equ : The two functions $H_{(0)}$ and Z_0 are strangely in reverse order. Everywhere else in the book the $x_<$ function is put on the left of the $x_>$ function.
- p 243 the 4th equ should have $-\delta(x-\xi)/x$ on the left // not $\delta(x-\xi)/x$
- p 243 the 6th equ left side should be $-f(x)$ // not $f(x)$
- p 243 the 6th equ should have $F_w(\mu)$ added to the integrand
- p 248* 4th equ should have factors $f_{2,k}$ and then $f_{1,k}$ // not $f_{1,k}$ then $f_{2,k}$
- p 250 last integral in (7.122) should have $a + (1/2)\int$ // not $-(1/2)\int$
- p 252* 4th equ, the integration should be $\int_0^{t0}$ // not $\int_0^t$
- p 254 the K = equation should have $f_1(x)$ in the integrand // not $f(x)$
- p 258 the w_k = triplet above (7.137) should have sinh and sin // not cosh and cos
- p 260 1st of equ (7.141) triplet, should have $-\nabla^2 v = 0$ // not $-\partial^2 v / \partial x^2 = 0$
- p 270* 2nd line should read in (7.163) and // not in (7.164) and
- p 271* equ (7.170) is missing the $H_\alpha^{(1)}(\sqrt{\lambda} r_>)$ factor which appears in (7.169)

- p 273* equ (7.176) should contain factor $\tilde{f}(\gamma)$ // not $\bar{f}(\gamma)$
- p 273 text line above equ 7.177 should say by $K_{i\gamma}(kr)$ // not by $rK_{i\gamma}(kr)$
- p 273* last equation should have $\sinh(\pi\gamma)$ // not $\sin(k\gamma\pi)$
- p 275* Equ after At $\varphi=0$ we have should have $\sinh(\gamma\pi)$ // not $\sin(\gamma\pi)$
- p 275* Equ after At $\varphi=2\pi$, should have $\sinh(\gamma\pi)$ // not $\sin(\gamma\pi)$
- p 275* the equ after We deduce that should read
- $$\tilde{v} = - \frac{\cosh[\gamma(\varphi-\pi)]}{\gamma \sinh(2\gamma\pi)} K_{i\gamma}(kr_0) \quad // \text{ not the very different expression shown.}$$
- p 277 equ (7.192) the radical in the left side exponent should be $\sqrt{r^2 + z^2}$, not $\sqrt{r^2 - z^2}$
- p 279* equ after (7.200), the radical exponent should be $\sqrt{r^2 + z^2}$, not $\sqrt{r^2 - z^2}$. This is OK in the following equation.
- p 289* first equ in the In Region I: should read 0 , $0 < t < R$ // the 0 , is missing
In other words it should look the way it looks for Region II.
- p 317* start of 2nd paragraph should read let $a(\omega) = 1/(1+\omega^2)$ // not $1/1+\omega^2$
- p 318 4th equ, left side should be $b_+(\omega)/b_-(\omega)$ // not $b_+(\omega) + b_-(\omega)$
- p 319 first equ should have 2 in the numerator // not 1 in numerator
- p 321* 2nd line of text should say the integral by closing the contour // not by choosing the contour
- p 322 equ (7.300), the factor $1/(2\xi)$ in the first integral should be $1/(2\pi)$
- p 325* first line of text should say Setting $\alpha = -iR$ // not $\alpha = iR$
- p 330 Ex 7.54, 2nd equ should have leading factor $\pi/\sqrt{p+k}$ // not $\pi/(p+k)$